

ATOMIC ENERGY CENTRAL SCHOOLS

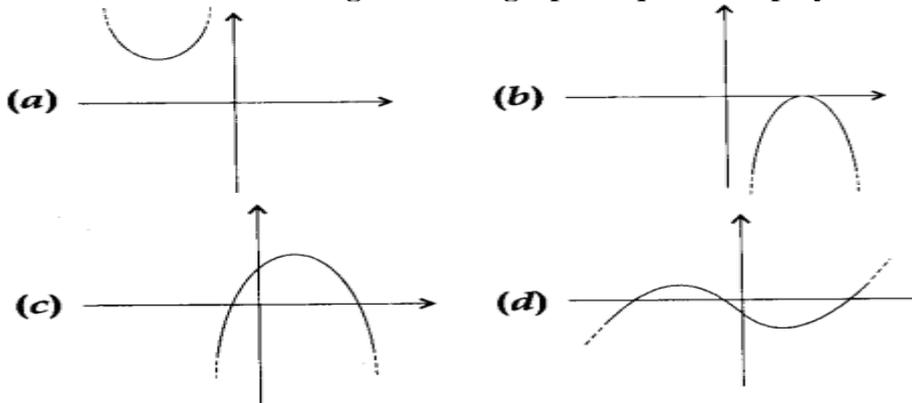
Class : 10 Sub : Mathematics Ch 2 Polynomials

SECTION A ( 1 X 12 = 12 )

Fill in the blanks with the correct options.

1. If one zero of the quadratic polynomial  $x^2 + 3x + k$  is 2, then the value of  $k$  is \_\_\_\_\_.  
(a) 10                      (b) -10                      (c) 5                      (d) -5
2. If the zeroes of the quadratic polynomial  $x^2 + (a + 1)x + b$  are 2 and -3, then \_\_\_\_\_.  
(a)  $a = -7, b = -1$     (b)  $a = 5, b = -1$     (c)  $a = 2, b = -6$     (d)  $a = 0, b = -6$
3. The number of polynomials having zeroes as 2 and -3 is \_\_\_\_\_.  
(a) 1                      (b) 2                      (c) 3                      (d) more than 3
4. A quadratic polynomial, whose zeroes are -4 and -5, is \_\_\_\_\_.  
(a)  $x^2 - 9x + 20$     (b)  $x^2 + 9x + 20$     (c)  $x^2 - 9x - 20$     (d)  $x^2 + 9x - 20$
5. The zeroes of the quadratic polynomial  $x^2 + 20x + 75$  are \_\_\_\_\_.  
(a) both negative    (b) one positive and one negative    (c) both positive    (d) both equal
6. What is the quadratic polynomial whose sum and the product of zeroes is  $\sqrt{2}, \frac{1}{3}$  respectively?  
(a)  $3x^2 - 3\sqrt{2}x + 1$     (b)  $3x^2 + 3\sqrt{2}x + 1$     (c)  $3x^2 + 3\sqrt{2}x - 1$     (d) None of the above
7. If  $p(x) = ax^2 + bx + c$ , then  $\frac{c}{a}$  is equal to \_\_\_\_\_.  
(a) 0                      (b) 1                      (c) sum of zeroes                      (d) product of zeroes
8. If  $p(x) = ax^2 + bx + c$ , then  $-\frac{b}{a}$  is equal to \_\_\_\_\_.  
(a) 0                      (b) 1                      (c) sum of zeroes                      (d) product of zeroes
9. A quadratic polynomial whose one zero is 6 and sum of the zeroes is 0, is  
(a)  $x^2 - 6x + 2$     (b)  $x^2 - 36$     (c)  $x^2 - 6$     (d)  $x^2 - 3$

10. Which of the following is not the graph of quadratic polynomial?



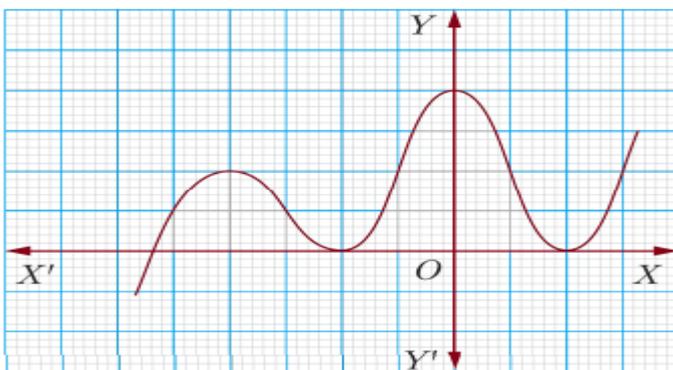
11. Assertion: The graph of quadratic polynomial  $p(x)$  intersect  $x$ -axis at two points.

Reason: The degree of quadratic polynomial is 2.

- a) Both Assertion and Reason are true and reason is the correct explanation of Assertion
- b) Both Assertion and Reason are true but reason is not the correct explanation of Assertion
- c) Assertion is true but Reason is false.
- d) both Assertion and Reason are false.

12. Assertion: The graph  $y=f(x)$  is shown in figure, for the polynomial  $f(x)$ . The number of zeroes of  $f(x)$  is 3.

Reason: The number of zeroes of the polynomial  $f(x)$  is the number of point of which  $f(x)$  cuts or touches the axes.



**SECTION B ( 2 X 10 = 20 )**

1. Find the zeroes of the polynomial  $f(x) = x^2 + 4x + 4$ .
2. For what value of  $k$ , is  $-2$  a zero of the polynomial  $3x^2 + 4x + 2k$ ?
3. Find a quadratic polynomial whose zeroes are  $3 +$  and  $-3$ .
4. If  $\alpha, \beta$  are the zeroes of a polynomial, such that  $\alpha + \beta = 6$  and  $\alpha\beta = 4$ , then write the polynomial.
5. If  $\alpha$  and  $\beta$  are zeroes of a polynomial  $x^2 + 6x + 9$ , then form a polynomial whose zeroes are  $-\alpha$  and  $-\beta$ .

6. The quadratic polynomial  $2x^2 - 3x + 1$  has zeroes as  $\alpha$  and  $\beta$ . Now form a quadratic polynomial whose zeroes are  $3\alpha$  and  $3\beta$ .
7. Find the roots of  $x^2 - 2x - 8$ .
8. Find the zeroes of  $x^2 - 2x$ .
9.  $\alpha$  and  $\beta$  are zeroes of the quadratic polynomial  $x^2 - 6x + y$ . Find the value of 'y' if  $3\alpha + 2\beta = 20$ .
10. Find a quadratic polynomial with  $\frac{1}{4}$  as the sum and  $-1$  as the product of its zeroes, respectively.

#### SECTION C ( 3 X 5 = 15 )

1. Find the zeroes of the polynomial  $f(u) = 4u^2 + 8u$ , and verify the relation between the zeroes and its coefficients.
2. If one root of the polynomial  $f(x) = 5x^2 + 13x + k$  is reciprocal of the other, then find the value of  $k$ .
3. If  $\alpha, \beta$  are the zeros of the polynomial  $2y^2 + 7y + 5$ , write the value of  $\alpha + \beta + \alpha\beta$ .
4. If  $\alpha$  and  $\beta$  are the zeros of the polynomial  $f(x) = x^2 - 5x + k$  such that  $\alpha - \beta = 1$ , find the value of  $k$ .
5. If the product of zeroes of the polynomial  $ax^2 - 6x - 6$  is 4, find the value of  $a$ . Find the sum of zeroes of the polynomial.

#### SECTION D ( 5 X 5 = 25 )

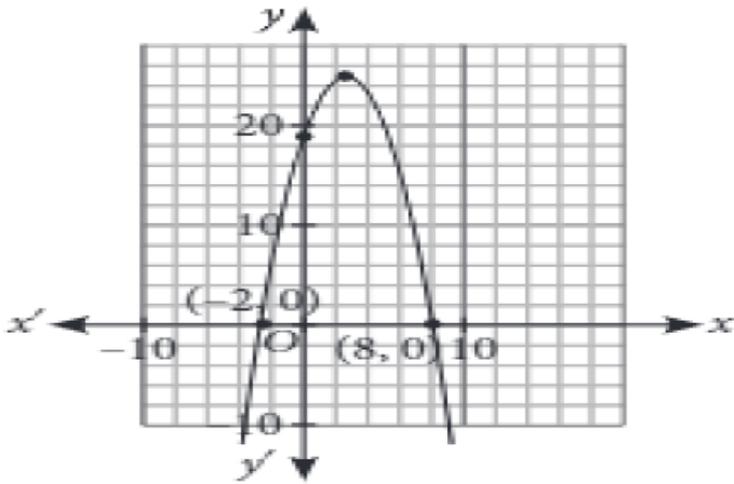
1. If  $\alpha$  and  $\beta$  are the zeroes of the polynomial  $p(x) = 2x^2 + 5x + k$ , satisfying the relation,  $\alpha^2 + \beta^2 + \alpha\beta = \frac{21}{4}$  then find the value of  $k$ .
2. Find a quadratic polynomial whose zeroes are reciprocals of the zeroes of the polynomial  $f(x) = ax^2 + bx + c$ ,  $a \neq 0$ ,  $c \neq 0$ .
3. If  $\alpha$  and  $\beta$  are zeroes of  $p(x) = kx^2 + 4x + 4$ , such that  $\alpha^2 + \beta^2 = 24$ , find  $k$ .
4. If  $p$  and  $q$  are the zeroes of  $x^2 + px + q$ , then find the values of  $p$  and  $q$ .
5. Find  $\alpha^{-1} + \beta^{-1}$ , if  $\alpha$  and  $\beta$  are zeroes of the polynomial  $9x^2 - 3x - 2$ .

#### SECTION E ( 4 x 2 = 8 )

#### CASE STUDY BASED QUESTION – 1

Mont Blanc Tunnel which is a highway tunnel between France and Italy, under the Mont Blanc Mountain in the Alps, and has a parabolic cross-section. The mathematical representation of the tunnel is shown in the graph.



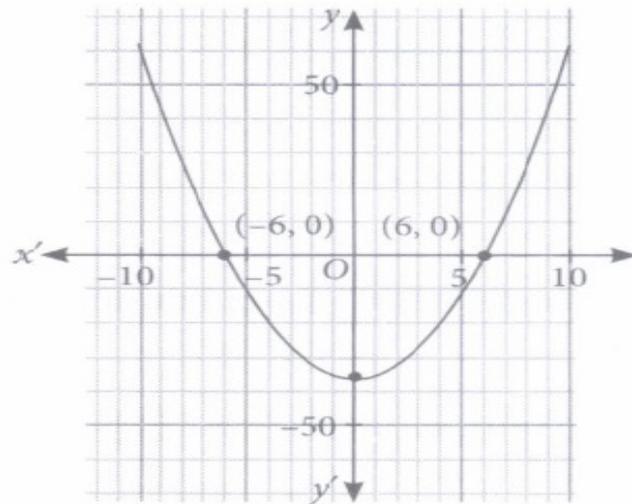


Based on the above information, answer the following questions.

- (1) What are the zeroes of the polynomial whose graph is given? (1)
- (2) What will be the expression of the polynomial given in diagram? (1)
- (3) What is the value of the polynomial represented by the graph, when  $x = 4$ ? (2)

#### CASE STUDY BASED QUESTION – 2

The shape of the honeycomb formed is that of a parabola. The mathematical representation of the honeycomb structure is shown in the graph.



Based on the above information, answer the following questions.

- (i) Which polynomial is represented by the graph? (1)
- (ii) Find the value of the polynomial represented by the graph when  $x = 6$ . (1)
- (iii) If the sum of zeroes of polynomial  $at^2 + 5t + 3a$  is equal to their product, then find the value of  $a$ . (2)